

To convert 2^{32} bytes (4,294,967,296 bytes) into gigabytes (GB), we divide it by $1,024^3$ (or 1,024 three times—):

$$4,294,967,296 \text{ bytes} / 1,024^3 = 4 \text{ GB}$$

So, 2^{32} is equal to 4 gigabytes

1 Megabyte (MB): In computing, 2^{20} bytes are often referred to as 1 Megabyte (MB). This is part of how data storage is measured:

- 2^{10} = 1,024 bytes is 1 Kilobyte (KB).
- 2^{20} = 1,048,576 bytes is 1 Megabyte (MB).

For example, consider a system with a 32-bit logical address space. If the page size in such a system is 4 KB (2^{12}), then a page table may consist of over ($2^{20} = 2^{32}/2^{12}$).

One simple solution to this problem is to divide the page table into smaller pieces. A logical address is divided into a page number consisting of 20 bits and a page offset consisting of 12 bits. Because we page the page table, the page number is further divided into a 10-bit page number and a 10-bit page offset.

Example: Process Pages

Imagine a program is being executed, and it is divided into pages to fit into memory. Here's a simple example:

Program Example

Let's say you have a program to calculate the sum of an array:

```
#include <stdio.h>
int main() {
    int arr[1000], sum = 0;
    for (int i = 0; i < 1000; i++) {
        arr[i] = i;
        sum += arr[i];
    }
    printf("Sum: %d\n", sum);
    return 0;
}
```

How This Program is Divided into Pages:

1. Code Segment: The part of the program containing the compiled instructions (e.g., the loop and logic for summing the array).

Let's assume this is Page 0

2. Data Segment The part of memory holding global variables (e.g., 'arr' and 'sum'). This becomes Page 1.

3. Stack Segment: The memory for function calls and local variables. This is Page 2.

4. Heap Segment: Dynamically allocated memory (not used in this program, but would be another page if necessary).

How Pages Are Mapped:

Logical Pages:

- Page 0: Contains the code segment.
- Page 1: Contains the array and global variables.
- Page 2: Contains stack data.

Physical Frames: These pages are mapped to frames in physical memory using the page table.

Logical Page	Physical Frame
Page 0	Frame 3
Page 1	Frame 1
Page 2	Frame 0

Accessing Data Using Logical Address:

Suppose the program accesses the 500th element of the array ('arr[500]'):

1. Logical Address: Let's say the address is 6,000 bytes.

- Page Number (p): $(6,000 \div 4,096 = 1)$ (Page 1 contains the array).
- Page Offset(d): $(6,000 \bmod 4,096 = 1,904)$.

2. Physical Address Calculation:

- Page Table maps Page 1 to Frame 1.
- Frame 1's starting physical address = $(4,096)$.
- Physical Address = $(\{\text{Frame Base}\} + \{\text{Page Offset}\} = 4,096 + 1,904 = 6,000)$.

Thus, the logical address translates to the physical address 6,000 bytes in physical memory.

Why Paging is Beneficial

Paging allows the operating system to load only the required pages into memory, improving memory utilization. For example:

- If the program doesn't use dynamic memory allocation, no heap pages need to be loaded.
- Pages can be swapped in and out of physical memory as needed (this is known as demand paging).

4096 represents the size of a single page in memory, and it's measured in bytes. This value corresponds to 4 KB** (as 1 KB = 1024 bytes).

Operating systems often use a page size of 4 KB because it strikes a balance between efficient memory management and performance. For example:

- Smaller pages mean less wasted memory if a process doesn't use all the data in a page.
- Larger pages improve performance since fewer pages need to be managed, but they could lead to unused memory within a page.

The exact size can vary depending on the system architecture or operating system. In the earlier example, 6000 represents a logical address within the program's memory space. Logical addresses are generated by the CPU during program execution and are part of the program's view of memory, irrespective of where data resides in physical memory.

The logical address 6000 bytes corresponds to a specific location within the program's logical memory.

- Based on the example provided:
 - A page size is 4096 bytes (4 KB)
 - Logical Address 6000 falls on Page 1 with an offset of ($6000 \bmod 4096 = 1904$) bytes within that page.

It demonstrates how a logical address can be mapped to a physical address using paging. In the example, 6000 represents a logical address in memory. Whether it maps to Page 1 depends on the page size and the way logical addresses are divided into pages.

Here's the Breakdown:

1. Page Size: The page size in the example is 4096 bytes (4 KB)
 - This means each page in logical memory spans a range of 4096 addresses.
2. Dividing Logical Address 6000:
 - To determine the Page Number divide the logical address by the page size:
 $\text{Page Number} = \text{Logical Address} / \text{Page Size} = 6000 / 4096 = 1.46$
 - Only the integer part of this division matters, which is 1. So, logical address 6000 belongs to Page 1
3. Offset Calculation:
 - The **Page Offset** is the remainder when dividing the logical address by the page size:
 $\text{Page Offset} = \text{Logical Address} \bmod \text{Page Size} = 6000 \bmod 4096 = 1904$
 - This offset shows the specific location within Page 1 (1904 bytes from the start of the page).

Visualization:

If logical memory is divided into pages of 4 KB each:

- Page 0: Addresses 0 to 4095.
- Page 1: Addresses 4096 to 8191.
- Page 2: Addresses 8192 to 12287.
- Page 3: Addresses 12288 to 16383.

Logical address 6000 falls in the range of Page 1 (4096–8191).

This logic ensures that we correctly map logical addresses to pages and calculate their offset. In this example, Page 0 represents the first page in logical memory, covering the range of addresses from 0 to 4095 (since the page size is 4096 bytes, or 4 KB).

Page 0 Details

- It contains the first 4096 bytes of the program's logical memory.
- Typically, in many programs, Page 0 might hold:

- The code segment, which includes instructions for the program (e.g., loops, function calls, and basic logic).
- Alternatively, it could store part of the global variables or other data, depending on how the program's memory is organized.

In the physical memory, the mapping is determined by the page table. If the page table maps Page 0 to Frame 3, the physical addresses for this page would start at the address of Frame 3 in physical memory.